## Your choices:

Test chosen: Sample size for unpaired $t$ test
Expected SD of each group $=65$
Significance level (alpha) $=0.05$ (two-tailed)

## Detailed explanation:

You requested a detailed explanation for $\mathrm{N}=25$ and power $=80 \%$.
Assume that the true difference between means is 52.68 . Now imagine that you perform many experiments, with $\mathrm{N}=25$ per group in each experiment. Due to random sampling, you won't find that the difference between means equals 52.68 in every experiment.
Instead, you'll find that the difference between means will be greater than 52.68 in about half the experiments, and less than 52.68 in the other half.

In $80 \%$ (the power) of those experiments, the P value will be less than 0.05 (two-tailed) so the results will be deemed "statistically significant". In the remaining $20 \%$ of the experiments, the difference between means will be deemed "not statistically significant", so you will have made a Type II (beta) error.

Summary: A sample size of 25 in each group has a $80 \%$ power to detect a difference between means of 52.68 with a significance level (alpha) of 0.05 (two-tailed).

## Alternative explanation using confidence intervals:

If you perform many experiments with $\mathrm{N}=25$ in each group, you expect that in $80 \%$ of these experiments (the power), the width of the $95 \%$ confidence interval for the difference between means will extend 52.68 or less in each direction. In the remaining $20 \%$ of the experiments, you will expect the $95 \%$ confidence interval to be wider than that.

## Table of tradeoffs:

For any combination of sample size $(\mathrm{N})$ and power, this table shows the difference between means that can be detected.

|  | Power |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| N per group | $\mathbf{9 9 \%}$ | $\mathbf{9 5 \%}$ | $\mathbf{9 0 \%}$ | $\mathbf{8 0 \%}$ | $\mathbf{5 0 \%}$ |
| 3 | 289.41 | 243.40 | 218.87 | 189.17 | 132.34 |
| 4 | 232.76 | 195.76 | 176.03 | 152.14 | 106.43 |
| 5 | 200.19 | 168.36 | 151.40 | 130.85 | 91.54 |
| 6 | 178.37 | 150.01 | 134.89 | 116.59 | 81.56 |


| 7 | 162.44 | 136.61 | 122.84 | 106.17 | 74.28 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 8 | 150.14 | 126.27 | 113.54 | 98.13 | 68.65 |
| 9 | 140.28 | 117.97 | 106.08 | 91.69 | 64.14 |
| 10 | 132.14 | 111.13 | 99.93 | 86.37 | 60.42 |
| 12 | 119.37 | 100.39 | 90.28 | 78.02 | 54.58 |
| 14 | 109.72 | 92.27 | 82.97 | 71.71 | 50.17 |
| 16 | 102.08 | 85.85 | 77.20 | 66.72 | 46.68 |
| 18 | 95.84 | 80.61 | 72.48 | 62.65 | 43.83 |
| 20 | 90.63 | 76.22 | 68.54 | 59.24 | 41.44 |
| 25 | 80.59 | 67.78 | 60.95 | 52.68 | 36.85 |
| 30 | 73.29 | 61.64 | 55.42 | 47.90 | 33.51 |
| 35 | 67.67 | 56.91 | 51.17 | 44.23 | 30.94 |
| 40 | 63.17 | 53.13 | 47.77 | 41.29 | 28.88 |
| 50 | 56.34 | 47.38 | 42.61 | 36.83 | 25.76 |
| 60 | 51.34 | 43.17 | 38.82 | 33.55 | 23.47 |
| 70 | 47.47 | 39.92 | 35.90 | 31.02 | 21.70 |
| 80 | 44.36 | 37.30 | 33.54 | 28.99 | 20.28 |
| 90 | 41.79 | 35.14 | 31.60 | 27.31 | 19.11 |
| 100 | 39.62 | 33.32 | 29.96 | 25.89 | 18.12 |
| 150 | 32.29 | 27.16 | 24.42 | 21.10 | 14.76 |
| 200 | 27.94 | 23.50 | 21.13 | 18.26 | 12.77 |
| 300 | 22.79 | 19.17 | 17.23 | 14.90 | 10.42 |
| 400 | 19.73 | 16.59 | 14.92 | 12.89 | 9.02 |
| 500 | 17.64 | 14.84 | 13.34 | 11.53 | 8.07 |
| 1000 | 12.47 | 10.48 | 9.43 | 8.15 | 5.70 |

## If you want to use unequal N :

Instead of using 25 subjects in each group, you can use unequal N. Substitute any of the following experimental designs, without losing any statistical power. Note that total sample size increases if you use unequal N (you must increase N for Group B more than you decrease N for group A ). This can make sense if treatment A "costs" more (considering expense, hassle and risk) than treatment B. Even though the total sample size goes up, choosing unequal N may reduce the total cost (or risk) of the experiment.

## Sample size

| Group A | Group B | Ratio | Total | When to choose <br> 25 |
| :---: | :---: | :---: | :---: | :--- |
| 25 | 1.000 | 50 | If the "cost" of treatment A is 1.0 times <br> the "cost" of treatment B. |  |
| 23 | 29 | 1.250 | 52 | If the "cost" of treatment A is 1.6 times <br> the "cost" of treatment B. <br> If the "cost" of treatment A is 2.3 times <br> the "cost" of treatment B. |
| 21 | 32 | 1.500 | 53 | 57 |
| 19 | 38 | 2.000 | If the "cost" of treatment A is 4.0 times <br> the "cost" of treatment B. |  |
| 17 | 51 | 3.000 | 68 | If the "cost" of treatment A is 9.0 times <br> the "cost" of treatment B. |
| 16 | 64 | 4.000 | 80 | If the "cost" of treatment A is 16.0 times <br> the "cost" of treatment B. |
| 15 | 75 | 5.000 | 90 | If the "cost" of treatment A is 25.0 times <br> the "cost" of treatment B. |

You cannot reduce the sample size of Group A to fewer than half the number needed if you choose equal sample size (without losing statistical power).

